

# Modelling and Reasoning in Metamodelling Enabled Ontologies\*

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**Abstract.** Ontologies are expected to play an important role in many application domains, as well as in software engineering in general. One problem with using ontologies within software engineering is that while UML, a widely used standard for specifying and constructing the models for a software-intensive system, has a four-layer metamodelling architecture, the standard Web Ontology Language (OWL) does not support reasoning over layered metamodels. OWL2 provides simple metamodelling by using a punning approach, however, the interpretation function is different based on the context, which leads to non-intuitive results. The OWL FA Language has a well defined metamodelling architecture. However, there is no study and tool for support reasoning over OWL FA. In this paper, we discuss some reasoning tasks in OWL FA. We also introduce the OWL FA Tool kit, a simple tool kit for manipulating and reasoning with OWL FA.

## 1 Introduction

Metamodelling appeals in many applications areas (such as UML [11], Model Driven Architecture [2], XML [13] and E-Commerce). It is not only the underpinning of modelling languages such as UML, but also central to OMG's MDA-based computing.

The W3C Web Ontology Language (OWL) [10] in combination with reasoning is already used in various other research areas like in model-driven software engineering in order to exploit the expressiveness of OWL and the usage of inference. However, the lack of a formal OWL language or OWL extension which supports metamodelling is an obstacle for the usage of OWL in other complex application areas.

The Resource Description Framework (RDF) and OWL Full support metamodelling by allowing users to use the built-in vocabulary without restrictions, which introduces an undecidability problem. OWL [10] provides formal semantics focused on conceptual modelling and adaptability of inference using DL reasoners and reasoning algorithms, but OWL does not support layered reasoning. OWL 2 provides simple metamodelling with semantics which correspond to

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\*This paper is an extended version of [5] which was presented at the International workshop on OWL: Experience and Directions (OWL-ED2009).

the contextual semantics defined in [6], however, it has been shown in [9] that these can lead to non-intuitive results.

For example, the following axioms state that *Eagle* is an *Endangered* species, and that *Harry* is an *Eagle*:

$$\text{ClassAssertion}(\text{Endangered Eagle}) \quad (1)$$

$$\text{ClassAssertion}(\text{Eagle Harry}) \quad (2)$$

The axioms 1, 2 could be interpreted by DL reasoner as follows:

$$\text{ClassAssertion}(\text{Cls} - \text{Endangered Ind} - \text{Eagle}) \quad (3)$$

$$\text{ClassAssertion}(\text{Cls} - \text{Eagle Ind} - \text{Harry}) \quad (4)$$

The names of concepts and individuals do not interact with each other even they are sharing the same name, e.g. *Eagle* is represented as individual by the name *Ind – Eagle* and as class by the name *Cls – Eagle*. This kind of metamodelling is often referred to as punning. Let us consider the following axioms:

$$\text{SameIndividuals}(\text{Aquila Eagle}) \quad (5)$$

$$\text{ClassAssertion}(\text{not}(\text{Aquila Harry})) \quad (6)$$

The axioms 5, 6 could be safely added to the ontology in contextual semantics, but under layered semantics this ontology is inconsistent because 5 indicates the meta-individual equality since the axiom  $\text{Eagle} \approx \text{Aquila}$  indicates the equivalence of the two concepts *Eagle* and *Aquila*. However, axiom 6 describes that *Harry* is not in *Aquila* which leads to the contradiction in combination with axiom 4.

In this paper, we present modelling and reasoning algorithms for OWL FA knowledge bases. For the reasoning service, an OWL FA ontology is transformed to a set of OWL DL ontologies, then existing DL reasoners are applied to the transformed knowledge base. The syntax and semantics of OWL FA is described in Section 2. Modelling in OWL FA is demonstrated in Section 3. In Section 4 reasoning in OWL FA is described. This contains a reduction to OWL DL knowledge bases and reasoning algorithms in order to propagate conditions between different modelling layers. Features of OWL FA Tool Kit are detailed in Section 5. The early evaluation are presented in Section 6. Then, related work and direction of OWL FA are discussed in Section 7 and Section 8 respectively.

## 2 OWL FA syntax and semantics

OWL FA [9] enables metamodelling. It is an extension of OWL DL, which refers to the description logic  $\mathcal{SHOIN}(\mathcal{D})$ . Ontologies in OWL FA are represented in

a layered architecture. This architecture is mainly based on the architecture of RDFS(FA) [8].

OWL FA specifies a layer number in class constructors and axioms to indicate the layer they belong to.

Let  $CN \in \mathbf{V}_{C_i}$  be an atomic class name in layer  $i$  ( $i \geq 0$ ),  $R$  an OWL FA-property in layer  $i$ ,  $o \in \mathbf{I}$  an individual,  $T \in \mathbf{V}_{DP}$  a datatype property name, and  $C, D$  OWL FA-classes in layer  $i$ . Valid OWL FA-classes are defined by the abstract syntax:

$$\begin{aligned}
C ::= & \top_i \mid \perp \mid CN \mid \neg_i C \mid C \sqcap_i D \mid C \sqcup_i D \mid \{o\} \mid \exists_i R.C \mid \\
& \mid \forall_i R.C \mid \leq_i nR \mid \geq_i nR \mid \\
& \text{(if } i = 1) \exists_1 T.d \mid \forall_1 T.d \mid \leq_1 nT \mid \geq_1 nT
\end{aligned}$$

The semantics of OWL FA is a model theoretic semantics, which is defined in terms of interpretations. In other words, the semantics of two layers which can be considered as TBox and ABox are same as in OWL DL. The idea of OWL FA is that the interpretation depends on the layer but is still an OWL DL interpretation. Given an OWL FA alphabet  $\mathbf{V}$ , a set of built-in datatype names  $\mathbf{B} \subseteq \mathbf{V}_D$  and an integer  $k \geq 1$ , an *OWL FA interpretation* is a tuple of the form  $\mathcal{J} = (\Delta^{\mathcal{J}}, \cdot^{\mathcal{J}})$ , where  $\Delta^{\mathcal{J}}$  is the domain (a non-empty set) and  $\cdot^{\mathcal{J}}$  is the interpretation. In the rest of the paper, we assume that  $i$  is an integer such that  $1 \leq i \leq k$ . The interpretation function can be extended to give semantics to OWL FA-properties and OWL FA-classes. Let  $RN \in \mathbf{V}_{AP_i}$  be an abstract property name in layer  $i$  and  $R$  be an abstract property in layer  $i$ . Valid OWL FA abstract properties are defined by the abstract syntax:  $R ::= RN \mid R^-$ , where for some  $x, y \in \Delta_{A_{i-1}}^{\mathcal{J}}$ ,  $\langle x, y \rangle \in R^{\mathcal{J}}$  iff  $\langle y, x \rangle \in R^{-\mathcal{J}}$ . Valid OWL FA datatype properties are datatype property names. The interpretation function is explained in detail in [9].

An interpretation  $\mathcal{J}$  satisfies an ontology  $\Sigma$  if it satisfies all the axioms in  $\Sigma$ .  $\Sigma$  is *satisfiable* (*unsatisfiable*) iff there exists (does not exist) such an interpretation  $\mathcal{J}$  that satisfies  $\Sigma$ . Let  $C, D$  be OWL FA-classes in layer  $i$ ,  $C$  is *satisfiable* w.r.t.  $\Sigma$  iff there exists an interpretation  $\mathcal{J}$  of  $\Sigma$  s.t.  $C^{\mathcal{J}} \neq \emptyset$ ;  $C$  subsumes  $D$  w.r.t.  $\Sigma$  iff for every interpretation  $\mathcal{J}$  of  $\Sigma$  we have  $C^{\mathcal{J}} \subseteq D^{\mathcal{J}}$ .

### 3 Modelling of Metamodelling Enabled Ontologies

In this section, we present the way to express metamodelling enabled ontologies in OWL 2. The layer information is encapsulated in custom annotation property called "Layer". This is different from [5] because we realise that creating a new syntax for OWL FA is unnecessary since we could store layer information as annotation properties. Moreover, this ontology conforms still to the OWL 2 syntax like the punning style which is another way to capture a simple modelling in OWL 2. Although, the layer numbers can/should be encapsulated by tools, there are two rules of thumb to help users to get the number right. Firstly, the subscript numbers are only used to indicate a sub-ontology (e.g.  $\mathcal{O}_2$ ), a constructor (e.g.  $\exists_2$ ), or axiom symbols (e.g.  $\sqsubseteq_2, :_2$ ) in a sub-ontology. Secondly, subscript

numbers of the constructors and axiom symbols indicate the sub-ontology that the class descriptions constructed by these constructors and axioms belong to.

The following example shows how to model an Endangered Species ontology with the DL syntax and then convert it into OWL 2 functional syntax. The main reason for using functional syntax is that it is obvious to see which layer they belong to.

*Example 1.* Endangered Species ontology expressed in DL syntax as follow:

$$\text{Eagle} \text{ :}_2 \text{ Endangered} \quad (7)$$

$$\text{Aquila} \text{ :}_2 \text{ Endangered} \quad (8)$$

$$\text{Aquila} \approx_2 \text{Eagle} \quad (9)$$

$$\text{Eagle} \sqsubseteq_1 \text{Bird} \quad (10)$$

$$\text{Aquila} \sqsubseteq_1 \text{Bird} \quad (11)$$

$$\text{Harry} \text{ :}_1 \text{Eagle} \quad (12)$$

*Example 2.* Endangered Species ontology expressed in OWL 2 syntax as follow:

$$\text{ClassAssertion(Annotation(Layer"2")Endangered Eagle)} \quad (13)$$

$$\text{ClassAssertion(Annotation(Layer"2")Endangered Aquila)} \quad (14)$$

$$\text{SameIndividuals(Annotation(Layer"2")Eagle Aquila)} \quad (15)$$

$$\text{SubClassOf(Annotation(Layer"1")Eagle Bird)} \quad (16)$$

$$\text{SubClassOf(Annotation(Layer"1")Aquila Bird)} \quad (17)$$

$$\text{ClassAssertion(Annotation(Layer"1")Eagle Harry)} \quad (18)$$

## 4 Reasoning in OWL FA

Now we briefly discuss some reasoning tasks in OWL FA. According to the layered architecture, the knowledge base  $\Sigma$  in OWL FA is divided into a sequence of knowledge bases  $\Sigma = \Sigma_1, \dots, \Sigma_k$ , whereas  $k$  is the number of layers. Since individuals in layer  $i + 1$  can be classes and properties in layer  $i$ , this also affects the axioms of the layer below. Hence, individual axioms in the knowledge base  $\Sigma_{i+1}$  can be considered as class axioms in the knowledge base  $\Sigma_i$ .

In an OWL FA knowledge base  $\Sigma$ ,  $\Sigma_2, \dots, \Sigma_k$  are *SHIQ* knowledge bases, i.e. nominals are not allowed. A nominal in a higher layer can lead to unsatisfiability of the knowledge bases. An interesting feature of  $\Sigma$  is that there could be interactions between  $\Sigma_i$  and  $\Sigma_{i+1}$ .

### 4.1 Preprocessing

In this section, we discuss how to reduce the reasoning problem in OWL FA into a reasoning problem in OWL DL.

**Definition 1.** Let  $\Sigma = \langle \Sigma_1, \dots, \Sigma_k \rangle$  be an OWL FA knowledge base, where each of  $\Sigma_1, \dots, \Sigma_k$  is consistent.  $\Sigma^* = \langle \Sigma_1^*, \dots, \Sigma_k^* \rangle$ , called the explicit knowledge base, is constructed by making all the implicit atomic class axioms, atomic property axioms, individual equality axioms explicit.  $\diamond$

As we have a finite set of vocabulary, we have the following Lemma.

**Lemma 1.** Given an OWL FA knowledge base  $\Sigma = \langle \Sigma_1, \dots, \Sigma_k \rangle$ . The explicit knowledge base  $\Sigma^*$  (OWL DL knowledge base) can be calculated from  $\Sigma$  in finite steps.

*Proof.* When  $k = 1$ , we can calculate the explicit knowledge base  $\Sigma_1^*$  in finite steps because the sets of names of classes (in layer 1), roles (in layer 1) and individuals are finite. When  $k > 1$ , let us assume that we can calculate the explicit knowledge bases  $\Sigma'_1, \dots, \Sigma'_i$  (where  $1 \leq i < k$ ) from  $\Sigma_1, \dots, \Sigma_i$  in finite steps. We add all the class and property equality axioms in  $\Sigma'_i$  to  $\Sigma_{i+1}$ . If the updated  $\Sigma_{i+1}$  is consistent. Then, we can make the implicit individual equality axioms (if any) explicit and add new class and property equality axioms into  $\Sigma'_i$ . Thus, we can calculate  $\Sigma''_1, \dots, \Sigma''_i$  in finite steps. As the individual names in  $\Sigma_{i+1}$  are finite, we can calculate the explicit knowledge bases  $\Sigma_1^*, \dots, \Sigma_{i+1}^*$  in finite steps.

Note that if a class description is not defined in  $\Sigma_i$  (i.e., if it is not equivalent to any atomic class), it is not represented by any meta-individual in  $\Sigma_{i+1}$ . This suggests the connections between  $\Sigma_i$  and  $\Sigma_{i+1}$  are atomic classes and properties in  $\Sigma_i$ , which are meta-individuals in  $\Sigma_{i+1}$ .

We now present the algorithm **Reduce**, that will reduce an OWL FA knowledge base  $\Sigma$  into a set of OWL DL knowledge bases  $\langle \Sigma_1^*, \dots, \Sigma_k^* \rangle$ . This algorithm is based on Definition 1 and Lemma 1. The algorithm takes an OWL FA KB  $\Sigma$  as input and returns a set of OWL DL KB  $\langle \Sigma_1, \dots, \Sigma_k \rangle$ . The Algorithm **Reduce** is shown in Algorithm 1.

The following theorem shows the termination of the algorithm **Reduce**, applied to an OWL FA KB  $\Sigma$ .

**Theorem 1.** Given an OWL FA knowledge base  $\Sigma = \langle \Sigma_1, \dots, \Sigma_k \rangle$ , then **Reduce**( $\Sigma$ ) terminates.

*Proof.* Termination of algorithm **Reduce** is straightforward from Lemma 1, which we can construct  $\langle \Sigma_1^*, \dots, \Sigma_k^* \rangle$  from  $\Sigma$  in finite step and a sets of class, property and individual equality axioms are finite. Thus, algorithm **Reduce** always terminates.

Here is the result from applying the Algorithm **Reduce** to the OWL FA KB  $\Sigma$ :

$$\Sigma_2 = \{\text{Endangered} : \text{Eagle}, \text{Endangered} : \text{Aquila}, \text{Eagle} = \text{Aquila}\}$$

$$\Sigma_1 = \{\text{Eagle} : \text{Harry}, \text{Eagle} \sqsubseteq \text{Bird}, \text{Aquila} \sqsubseteq \text{Bird}, \text{Aquila} \equiv \text{Eagle}\}$$

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**Algorithm 1** Reduce

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**Input:** OWL FA KB  $\Sigma$ **Output:** satisfiable and a set of OWL DL KB  $\langle \Sigma_1, \dots, \Sigma_k \rangle$ .

```
1: boolean satisfiable = true;
2: Collect axioms from the layer number and store in  $L_0, \dots, L_n$ 
3: Create knowledge base  $\Sigma_i = (L_0, L_1), \dots, \Sigma_k = (L_{n-1}, L_n)$ 
4: repeat
5:    $ce_i = \emptyset, pe_i = \emptyset$  and  $oe_i = \emptyset$ 
6:   Check consistency of  $\Sigma_i$  with DL reasoner
7:   if  $\Sigma_i$  is consistent then
8:     for each  $\Sigma_i^*$  ( $1 \leq i \leq k$ ) do
9:       Identify the new concept equality in  $\Sigma_i^*$  and store it in  $ce_i$ 
10:      Identify the new property equality in  $\Sigma_i^*$  and store it in  $pe_i$ 
11:      Identify the new individual equality in  $\Sigma_i^*$  and store it in  $oe_i$ 
12:      for each  $ce_i, pe_i$  and  $oe_i$  do
13:        if  $i = 1$  then
14:          Add  $ce_i$  and  $pe_i$  as individual equality into  $\Sigma_{i+1}^*$ 
15:        else if  $i = k$  then
16:          Add  $oe_i$  as property or concept equality into  $\Sigma_{i-1}^*$ 
17:        else
18:          Add  $ce_i$  and  $pe_i$  as individual equality into  $\Sigma_{i+1}^*$ 
19:          Add  $oe_i$  as property or concept equality into  $\Sigma_{i-1}^*$ 
20:        end if
21:      end for
22:    end for
23:  else
24:    satisfiable = false;
25:  end if
26: until ( $ce_i = \emptyset \ \& \ pe_i = \emptyset \ \& \ oe_i = \emptyset$ ) || satisfiable = false;
27: return  $\langle \Sigma_1, \dots, \Sigma_k \rangle$ .
```

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## 4.2 Consistency Checking

In this section, we present the algorithm **Consistent**, that will check the consistency of an OWL FA knowledge base  $\mathcal{O}$ . We can reduce an OWL FA knowledge base to a collection of OWL DL knowledge bases, therefore existing DL reasoner capabilities can be used. Consistency checking for OWL FA is done in two steps: First, we check the syntax of OWL FA. For example,  $\Sigma = \{C \sqsubseteq_2 D, C \sqsubseteq_3 E\}$  is non-well formed because in OWL FA we do not allow OWL class construct between layer except an instance-of relationship. Secondly, we check the consistency of each OWL DL-knowledge base that is computed from the OWL FA knowledge base with an existing DL reasoner. The Algorithm **Consistent** is shown in Algorithm 2.

We invite the reader to note that *check-dl-consistent* is a function call to a DL Reasoner.

**Theorem 2.** *Given an OWL FA knowledge base  $\Sigma = \langle \Sigma_1, \dots, \Sigma_k \rangle$ .  $\Sigma$  is consistent iff each  $\Sigma_i^*$  ( $1 \leq i \leq k$ ) is consistent.*  $\diamond$

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**Algorithm 2** Consistent

---

**Input:** OWL FA Knowledge Base  $\Sigma = \langle \Sigma_1, \dots, \Sigma_k \rangle$

**Output:** *true* if  $\Sigma$  is consistent, *false* otherwise

```
1: Ont =  $\emptyset$ 
2: Check OWL FA syntax
3: Ont = Reduce( $\Sigma$ );
4: for each  $\Sigma_i$  in Ont do
5:   check-dl-consistent( $\Sigma_i$ )
6:   if  $\Sigma_i$  is not consistent then
7:     Return false
8:   end if
9: end for
10: return true.
```

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Theorem 2 shows we can reduce the OWL FA-knowledge base consistency problem to the OWL DL-knowledge base consistency problem.

*Proof.* The consistency check of an OWL FA KB with Consistent( $\Sigma$ ) is straightforward from Lemma 1. We can construct  $\langle \Sigma_1^*, \dots, \Sigma_k^* \rangle$  from  $\Sigma$  in finite steps then we check the consistency for each  $\Sigma_i^*$  with a DL reasoner. Therefore, the OWL FA knowledge base  $\Sigma$  is consistent if and only if each  $\Sigma_i^*$  ( $1 \leq i \leq k$ ) is consistent.

Let us consider the following axiom by inserting it into OWL FA KB  $\Sigma$  (cf. example 2):

$$\text{ClassAssertion(Annotation(Layer"1")Not(Aquila) Harry)} \quad (19)$$

It is obvious to see that this axiom will make  $\Sigma_1^*$  inconsistent, which leads to an inconsistent OWL FA KB  $\Sigma$  because the meta-individual equality axiom  $\text{Eagle} \approx_2 \text{Aquila}$  indicates the equivalence of the two concepts **Eagle** and **Aquila**, and  $\text{Harry}^{\mathcal{J}}$  cannot be both in and not in  $\text{Eagle}^{\mathcal{J}}$ .

### 4.3 Instance Retrieval

Instance retrieval in OWL FA is trivial because after the reduction process, we get a set of OWL 2 DL ontology then we could perform instance retrieval against those ontologies. However, without specifying a target ontology, it is not efficient since, we have to go through all ontologies in a set. Therefore, we need a smart algorithm for instance retrieval for OWL FA, in order to select the right ontology that contains a target concept. Firstly, we need to search for a target concept in each ontology of the set. This step does not require any DL reasoner. Then, we could perform instance retrieval against a selected ontology with a DL reasoner. A formal definition of instance retrieval for OWL FA is given in Definition 2.

**Definition 2.** Given an ABox  $\mathcal{A}_i$  and a query  $Q$ , i.e., a concept expression, find all individuals  $a$  such that  $a$  is an instance of  $Q$ , i.e.,  $\{a \mid \forall a \in \mathcal{A}_i, a : Q\}$ .  $\diamond$

We present the instance retrieval for OWL FA in Algorithm 3. The algorithm *instanceOf* will take an OWL FA ontology  $\mathcal{O}$  and a concept  $C$  as input. The algorithm returns a set containing the instances of concept  $C$ .

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**Algorithm 3** instanceOf

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**Input:** OWL FA Knowledge Base  $\Sigma = \langle \Sigma_1, \dots, \Sigma_k \rangle$  and a concept  $C$

**Output:** A set contains instance of concept  $C$

```

1: ind =  $\emptyset$ 
2: Ont =  $\emptyset$ 
3: Ont = Reduce( $\Sigma$ );
4: for each  $\Sigma_i$  in Ont do
5:   if  $\Sigma_i$  contains  $C$  then
6:     ind = get-dl-instance-of( $\Sigma_i, C$ )
7:   end if
8: end for
9: return ind.
```

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Due to space limitations, we cannot describe all reasoning tasks for OWL FA in this paper, however, since we can reduce OWL FA into a set of OWL DL ontologies then all existing DL reasoner's capabilities can be used.

## 5 OWL FA Tool Kit

In this section, we introduce the OWL FA Tool Kit, a simple graphic user interface for modeller to create an OWL FA ontology and perform reasoning over it. The OWL FA Tool Kit contains features as follows:

- Editor - for checking the OWL FA ontology before performing the reasoning.
- Ontology Consistency Checker- for checking whether a given metamodelling enabled ontology is consistent.
- Concept Satisfiability Checker - for verifying whether a concept  $A$  is a non-empty set in a given OWL FA ontology  $\mathcal{O}$ .
- Query Answering - for accessing information form a given metamodelling enabled ontologies by using SPARQL queries.
- Export a collection of OWL DL to files.

## 6 Evaluation

In this section, we compare the metamodelling in OWL FA with OWL 2 as OWL 2 is the only OWL language that can support metamodelling and it has tools support.

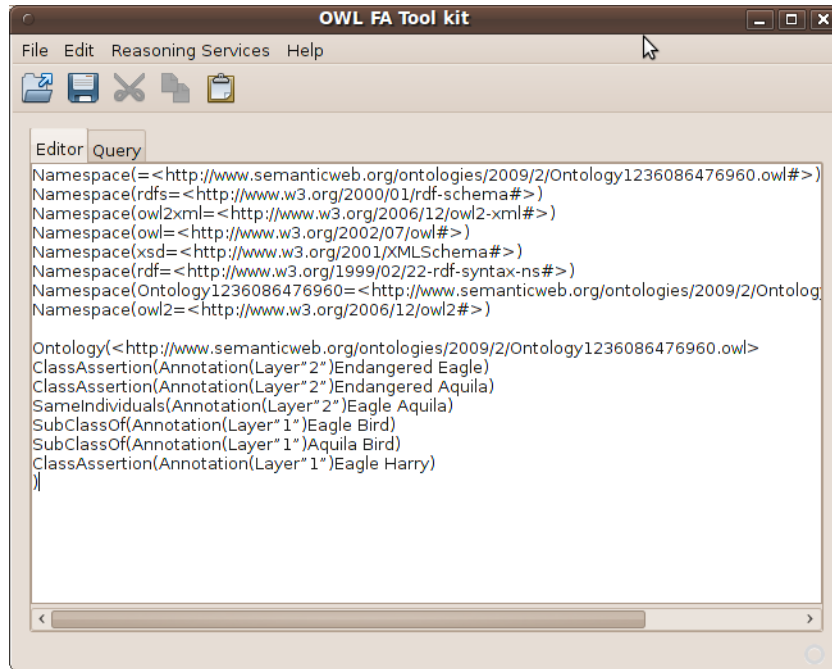


Fig. 1. OWL FA Tool Kit

### 6.1 Use case 1: Consistency checking

OWL 2 provides simple metamodelling with semantics which correspond to the contextual semantics defined in [6], however, it has been shown in [9] that these can lead to non-intuitive results.

Let us consider an ontology from Example 2 in Section 3 and the axioms 19. This ontology is consistent when we perform consistency checking with any existing DL reasoner. The existing DL reasoner does not take layer informations which are described as annotation property into account and it interpret this ontology with contextual semantics.

This ontology is inconsistent based on layered architecture in OWL FA as we described in Section 4. OWL FA Toolkit takes layer information into account and maintain a relationship between objects that sharing the same URI.

### 6.2 Use case 2: Instance retrieval

In OWL 2, if we do not provide the explicit instantiation between class and individual, it is difficult for any existing DL reasoner to discover those information because in contextual semantics, classes and individuals are interpreted independently. Let consider an ontology from Example 2 and remove axioms 14 and 15 from the ontology. Then, we would like to retrieve all objects that

belong to *Endangered*. Without adding an axiom to indicate that *Aquila* is an *Endangered* then, *Aquila* is not included in the answer set. Although, concept *Aquila* is equivalent to concept *Eagle* but the interpretation of concept *Eagle* and object *Eagle* are independent from each other. Therefore, the existing DL reasoner could not found the relation between *Aquila* and *Endangered*.

For OWL FA and our tool kit, it returns more complete answer sets because in the reduction process, we propagate all class and property equalities to be object equalities in the higher layer and propagate all object equalities to be class or property equalities in the lower layer.

## 7 Related Work

OWL FA was introduced in [9] as a metamodelling extension of OWL. Motik [6] addressed metamodelling in OWL with two different semantics. The contextual semantics (or  $\pi$ -semantics) uses punning, i.e. names are replaced by distinct names for concepts, individuals and roles. This is like the different representation of an object in the OWL DL ontologies  $\Sigma_i$  in OWL FA. OWL2 [7] provides simple metamodelling features which is based on the contextual approach. The other semantics is the HiLog semantics (or  $\nu$ -semantics). The HiLog semantics is stronger than the  $\pi$ -semantics. The concepts and individual interpretations are not independent.

De Giacomina et al. [4] proposed the HiDL – Lite language, which adds one layer on top of the DL-Lite $\mathcal{R}$  language. This supports meta-classes and meta-properties and presents the query answering algorithm by reducing HiDL – Lite to DL-Lite $\mathcal{R}$  with the intention of using an existing DL-Lite reasoner. In OWL FA the semantics of meta-level are same as domain knowledge unlike HiDL-Lite that semantics of the meta-level need to re-define.

Description Logic reasoning is applied to UML models in [1, 12, 3]. The models are transformed into DL representations. Reasoning is used to check consistency of models and between models. However, metamodels are not considered.

## 8 Discussion

In this section, we discuss the future direction of OWL FA. Although OWL FA has a well defined metamodelling architecture, OWL does not support cross layer constraints. Let's take the well known Endangered species as an example. One would like to define a constraint on a meta-concept **Endangered** that all instances of these meta-concept have only 3000 individuals. Therefore, if a concept **Eagle** is an instance of the meta-concept **Endangered**, the constraint should be applied to the concept **Eagle** as well. We have an idea how to express this kind of constraint by using a TopObjectProperty in OWL 2. We can then express this **Endangered** requirement as  $\top \sqsubseteq \leq 3000 \sqcup .\text{Endangered}$  then propagate this constraint to all instances of **Endangered**. This is beyond OWL FA so we would like to investigate on enriching OWL FA toward OWL 2 FA. Another issue is that, in the

cross layer constraints or restrictions for metamodelling in ontologies that we described in sections 2-5, we show that OWL FA is able to capture multiple layers better than OWL 2. However, the constraints or restrictions in OWL FA are relations between two layers. Let's consider an ObjectProperty assertion in layer  $M_2$ , `Endangered liveIn Continent`, which is expressed by the ObjectProperty `liveIn`. This constraint can only be used to validate the model between the layers  $M_2$  and  $M_1$ . We plan to investigate that it is possible to propagate the constraints across multiple layers. We are thinking about to use a meta prefix (`meta-`) like `meta.liveIn` that would still be an object property in the  $M_2$  layer and there the object property assertions in layer  $M_1$  remain unchanged like `liveIn(Eagle, Europe)`. However, we could also propagate this property assertion from model  $M_1$  semantically to model  $M_0$ . For instance the property assertion `meta.liveIn(Eagle, Europe)` in  $M_1$  becomes the subclass axiom `Eagle  $\sqsubseteq$   $\exists$  liveIn.Europe` in the model  $M_0$ . This would be very interesting because we could specify all the constraints only in higher layers, then propagate them down to the lower layers automatically.

## 9 Conclusion

In this paper, we reintroduce OWL FA language and demonstrate how to model the metamodelling enabled ontology, followed by a description of reasoning in OWL FA for different reasoning tasks. And the reduction from an OWL FA knowledge base into OWL DL knowledge bases algorithms are describes. These algorithms use standard DL reasoning as a black-box service. Based on the given examples, a metamodelling enables ontology is described in OWL 2 DL.

We have shown that we can make use of the existing DL reasoners to reason over OWL FA knowledge base. As we discussed in section 4, we can calculate the explicit OWL DL knowledge base  $\Sigma_i^*$  from OWL FA knowledge base  $\Sigma^*$ .

We have implemented the OWL FA Tool kit for modeller to manipulating and reasoning over OWL FA standard and plan to incorporate these into the TrOWL<sup>3</sup> reasoning infrastructure.

In the future, we would like to enrich OWL FA language toward the direction we described in discussion section in order to increase expressive power of the language such as propagate constraints between layers. Moreover, we would like to apply the fixed-layer architecture to OWL 2 DL which has more expressive power than OWL DL. And we plan to provide tools along with a reasoning mechanism for OWL 2 FA.

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