

# Formal Specification and Verification

## List of Topics

- **Propositional logic**

- Syntax, semantics
- Translation to CNF (also structure preserving translation; optimized translation)
- Methods for checking validity, satisfiability, entailment:
  - \* Inference Systems and Proofs - Example: Hilberts Deductive System
  - \* The Resolution Procedure
  - \* Sequent calculi
  - \* The DPLL procedure
  - \* BDDs; OBDDs.

- **First-order logic**

- Syntax, semantics
- Logical theories (Link theories - models)
- Herbrand models, Term algebras, free algebras

- **Specification**

- Algebraic specification
- Transition systems; Program graph representation; links

- **Verification**

- Temporal logic
  - \* LTL (syntax, semantics)
  - \* CTL (syntax, semantics)
  - \* Comparison between LTL and CTL
  - \* Model checking
    - Problem description
    - Algorithm which computes the set of states at which a CTL formula holds
    - Implementation based on OBDDs
- Propositional dynamic logic
  - \* Syntax, semantics
  - \* Axiom system for PDL:
    - Soundness and Completeness: definitions; proof idea;
    - Using a (given) axiom system for proving formulae in PDL.
  - \* Finite model property (Proof idea); decidability
  - \* Using a (given) sequent system for proving formulae in PDL.

- Deductive verification for infinite state systems: An introduction
  - \* Succinct representation of sets of states and of transitions between sets of states using formulae.
  - \* Verification problem: Program + Description of the bad states
    - Succinct representation using formulae
    - Initial state, error state, transition relation, computation,
    - Checking safety: compute set of reachable states
      - post operator (idea); iterations; Forward reachability analysis
      - pre operator (idea); Backward reachability analysis (idea)
  - \* Invariant checking, Bounded model checking (definitions)